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Total Number of Pages: 02

Course: B.Tech/IDD
Sub_Code: CSBS2001

3rd Semester Regular Examination: 2024-25

SUBJECT: Discrete Mathematics

BRANCH(S): CE, CSIT, CSEAI, CSE, CSE, CSEAIML, CSEDS, CST, IT

Time: 3 Hours

Max Marks: 100

Q.Code: R564

Answer Question No.1 (Part-I) which is compulsory, any eight from Part-II and any two from Part-III.

The figures in the right hand margin indicate marks.

Part-I

Q1 Answer the following questions: (2 x 10)

- Show that $p \vee (q \wedge r)$ and $(p \vee q) \wedge (p \vee r)$ are logically equivalent.
- Explain bijective function with an example.
- What rule of inference is used in this argument? If I study hard, then I get A's. I study hard. Therefore I get A's.
- In how many ways can a party of 5 men and 4 women be seated in a circular table so that no two women sit together?
- Define cyclic group. Give an example of it.
- Prove or disprove that every integral domain is a field.
- Define algebraic structures. Give an example of it.
- Define Hamiltonian circuits.
- Explain induced subgraph with a counter example.
- Define graph isomorphism with an example.

Part-II

Q2 Only Focused-Short Answer Type Questions- (Answer Any Eight out of Twelve) (6 x 8)

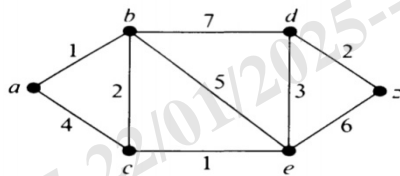
- Use mathematical induction to prove that $n^3 - n$ is divisible by 3 whenever n is a positive integer.
- Find $f \circ g$ and $g \circ f$, where $f(x) = x^2 + 1$ and $g(x) = x + 2$, both functions are from real numbers to real numbers.
- When we say a function invertible? Give an example of an invertible function.
- Find the particular solution of the recurrence relation $a_n + 5a_{n-1} + 6a_{n-2} = 3n^2$.
- How many poker hands of five cards can be dealt from a standard deck of 52 cards? Also how many ways are there to select 47 cards from a standard deck of 52 cards?
- Define partial ordering. Show that the inclusion relation \subseteq is a partial ordering on the power set of a set S .
- If G is a finite group and $a \in G$ then show that $o(a) | o(G)$.

- h) If G is a group such that $(a \cdot b)^2 = a^2 \cdot b^2$, for all $a, b \in G$, then show that G is abelian.
- i) Show that kernel of homomorphism is a normal subgroup.
- j) Show that a graph G is bipartite if it contains no cycle of odd length.
- k) Write a short note on Dijkstra's algorithm.
- l) Define vertex coloring. Prove that every planar graph is 6-vertex colorable.

Part-III

Only Long Answer Type Questions (Answer Any Two out of Four)

- Q3** a) Define propositional equivalence. Show that $(p \rightarrow q) \vee (p \rightarrow r)$ and $p \rightarrow (q \vee r)$ are Logically equivalent. **(8x2)**
- b) State Demorgan's laws. Using Venn diagrams prove it.
- Q4** a) Define Pigeon-hole principle. Students are awarded 4 grades A, B, C , and D . How many students must be there in a group so that at least 6 students get the same grade? **(8x2)**
- b) Define equivalence relation. Explain it with a suitable example.
- Q5** a) Show that a homomorphism ϕ of G onto \bar{G} with Kernel K_ϕ is an isomorphism of G into \bar{G} if and only if $K_\phi = (e)$. **(8x2)**
- b) Define right coset of a subgroup H in the group G . Show that there is a one-to-one correspondence between any two right cosets of H in G .
- Q6** a) Define Euler path and Eulerian circuit with example. Find shortest path from a to z in the following graph **(8x2)**



- b) Define minimum spanning tree. Find a minimum spanning tree of the following graph

